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# Selective oxidation of methane over $MoO_x/SiO_2$ : isolation of the kinetics of reactions occurring in the gas phase and on the surfaces of SiO<sub>2</sub> and MoO<sub>x</sub>

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## Abstract

The selective oxidation of methane to formaldehyde over  $MoO_x/SiO_2$  was investigated to identify the contributions of methane and formaldehyde reactions occurring in the gas phase and on the surfaces of  $SiO_2$  and dispersed  $MoO_x$  to the overall observed reaction rate. Experiments were conducted with 4.5 wt%  $MoO_3/SiO_2$  at a nominal surface concentration of 0.44 Mo nm<sup>-2</sup>. Data were acquired for  $CH_4/O_2$  ratios from 2 to 34 and temperatures from 848 to 923 K. Homogeneous oxidation of methane was negligible, and the homogeneous oxidation of formaldehyde contributed only to a small degree. The formation of formaldehyde was found to occur largely over  $MoO_x$  and only to a limited degree over SiO\_2. By contrast, the rates of formaldehyde consumption over  $MoO_x$  and SiO\_2 were comparable. For SiO\_2 the only process occurring was  $CH_2O$  decomposition, which was independent of the  $CH_4/O_2$  ratio, whereas in the case of  $MoO_x$ ,  $CH_2O$ decomposition was accompanied by combustion of the  $H_2$  formed and by direct  $CH_2O$  combustion principally to CO. A comprehensive model of the overall reaction kinetics was assembled from the kinetics determined for the reactions of methane and formaldehyde in the gas phase and on the surfaces of  $SiO_2$  and  $MoO_x$ . This model describes the observed rates of methane conversion and the formaldehyde selectivity measured experimentally as functions of temperature and  $CH_4/O_2$  ratio. This model is then used to determine the maximum single-pass yield of  $CH_2O$  for a given temperature and  $CH_4/O_2$  ratio. It is predicted that the maximum single-pass yield increases with reaction temperature and decreasing  $CH_4/O_2$  ratio.

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# 1. Introduction

The selective oxidation of methane to formaldehyde in a single step is a challenging problem of great practical importance [1]. Silica-supported oxides are among the bestperforming heterogeneous catalysts for the selective oxidation of methane, especially the supported oxides of Mo, V, and Fe [2–4]. Silica has emerged as the preferred support because other refractory supports, such as TiO<sub>2</sub> and Al<sub>2</sub>O<sub>3</sub>, burn formaldehyde very rapidly at temperatures well below those required for the activation of methane [5]. Although

\* Corresponding author. *E-mail address:* bell@cchem.berkeley.edu (A.T. Bell). SiO<sub>2</sub> is inert to CH<sub>2</sub>O relative to other supports, it still decomposes CH<sub>2</sub>O rapidly at temperatures and contact times relevant to methane oxidation [6]. Since the optimum metal loading needed to achieve maximum formaldehyde yield is well below monolayer coverage [2,7], most of the exposed surface area is SiO<sub>2</sub>. The loss of CH<sub>2</sub>O via homogeneous reaction is also known to occur [8,9] and has been implicated as a primary factor limiting CH<sub>2</sub>O yield during CH<sub>4</sub> oxidation over MoO<sub>x</sub>/SiO<sub>2</sub> [7]. However, previous studies modeling the kinetics of CH<sub>4</sub> oxidation over bare SiO<sub>2</sub> and MoO<sub>x</sub>/SiO<sub>2</sub> have ignored the gas-phase contribution to the CH<sub>2</sub>O reaction rate [10–13]. Therefore the question arises, how much of a role do the silica support and the gas phase play in determining the product distribution during methane oxidation over silica-supported oxides? The selective oxidation of methane to formaldehyde may be reduced to two processes, the formation and consumption of the product formaldehyde. The kinetics of formaldehyde consumption (i.e., decomposition and oxidation) have typically been studied indirectly by analysis of rate data for methane oxidation. However, we can obtain a better understanding of the kinetics of  $CH_2O$  decomposition and oxidation by studying these secondary processes independently of  $CH_4$  oxidation.

This study focuses on decoupling the rates of reaction occurring over  $MoO_x/SiO_2$ . The rates of  $CH_4$  oxidation and  $CH_2O$  consumption occurring in the gas phase, on the  $SiO_2$  support, and on the  $MoO_x$  sites are decoupled through kinetic analysis of  $CH_4$  oxidation and  $CH_2O$  reaction data obtained over a wide range of feed compositions and over a range of temperatures relevant to methane activation (> 848 K). The reaction network and rate laws utilized are justified by kinetic analysis. The individually measured kinetics are assembled to describe the relevant processes occurring during  $CH_4$  oxidation over  $MoO_x/SiO_2$ . The model is used to describe the effects of operating conditions on catalyst performance and to define the contributions of the gas phase, exposed support, and supported  $MoO_x$  to the overall rates of methane oxidation and formaldehyde consumption.

## 2. Experimental

A  $MoO_x/SiO_2$  catalyst was prepared by aqueous impregnation of Silicycle 60-Å silica gel with ammonium heptamolybdate (AHM) tetrahydrate (Aldrich 99.98% pure). The bare silica gel was washed in 9 M HNO<sub>3</sub> at 333 K, rinsed thoroughly with deionized water, and calcined in flowing air for 3 h at 973 K to remove alkaline earth impurities [14,15]. This treatment reduced the silica surface area from 500 to 460 m<sup>2</sup> g<sup>-1</sup>, as measured by five-point BET analysis of N<sub>2</sub> adsorption isotherms. AHM (0.067 g) was dissolved in 2.1 g of deionized water (150% of the pore-filling amount) for each gram of silica gel to be prepared. The silica and solution were mixed to dryness in a bath heated at 333 K, oven-dried at 383 K overnight, and calcined under flowing air at 873 K for 3 h before use. After loading with molybdena, the catalyst surface area was 426 m<sup>2</sup> g<sup>-1</sup>. Elemental analysis (Galbraith Laboratories) determined the Mo weight fraction to be 3.0% (4.5 wt% as MoO<sub>3</sub>), so that the nominal surface coverage of  $MoO_r$  was 0.44 Mo nm<sup>-2</sup>. The diameter of the catalyst particles was 200-500 µm, which was suffi-

Table 1		
Catalyst	physical	properties

ciently small to ensure that the reactions were not limited by mass transfer according to the Weisz–Prater criterion [16]. The catalyst was used without adjustment of the size distribution or dilution.

The catalyst properties are summarized in Table 1. The parameter  $\zeta$  describes the ratio of the exposed SiO<sub>2</sub> area per unit bed volume of the MoO<sub>x</sub>/SiO<sub>2</sub> catalyst to that of the bare SiO<sub>2</sub>, and is calculated as

$$\zeta = \frac{a_{\rm m}\rho_{\rm b}}{a_{\rm m}^0\rho_{\rm b}^0} \left(1 - \frac{c_{\rm m}}{c_{\rm m}^{\rm mono}}\right),\tag{1}$$

where  $a_{\rm m}$  and  $\rho_{\rm b}$  are the specific surface area and bulk density of the MoO<sub>x</sub>/SiO<sub>2</sub> catalyst, respectively, and  $a_{\rm m}^0$  and  $\rho_{\rm b}^0$  are the corresponding parameters for the bare SiO<sub>2</sub>. The term in parentheses accounts for the fraction of the surface of MoO<sub>x</sub>/SiO<sub>2</sub> occupied by MoO<sub>x</sub>.  $c_{\rm m}$  is the surface concentration of Mo, and  $c_{\rm m}^{\rm mono}$  is the theoretical monolayer coverage of MoO<sub>x</sub>, taken as 8.2 Mo nm<sup>-2</sup> [17]. The porosity  $\varepsilon$  is calculated from the bulk density  $\rho_{\rm b}$  and skeletal density  $\rho_{\rm s}$  of each catalyst as

$$\varepsilon = \frac{\rho_{\rm b}}{\rho_{\varepsilon}} = 1 - \frac{\rho_{\rm b}}{\rho_{\rm s}},\tag{2}$$

where  $\rho_b$  was measured by volumetry, and  $\rho_s$  was estimated from linear summation of skeletal densities of the SiO<sub>2</sub> and MoO<sub>x</sub>, assuming the MoO<sub>x</sub> to be present as bulk MoO<sub>3</sub>:

$$\rho_{\rm s} = (2.20 \text{ g cm}^{-3})(1 - \omega_{\rm MoO_3}) + (4.62 \text{ g cm}^{-3})\omega_{\rm MoO_3},$$
(3)

where  $\omega_{MoO_3}$  is the weight fraction of MoO<sub>x</sub> as MoO<sub>3</sub>.

Raman spectra were recorded with a Kaiser Optical HoloLab 5000 series Raman spectrometer equipped with a Nd:YAG laser that was frequency-doubled to 532 nm and operated at 7 mW. Catalyst samples (50–100 mg) were ground into powder and pressed into discs 1 cm in diameter at 10,000 psi. The discs were placed in a sealed rotary cell and rotated at 400 rpm during laser exposure to distribute the beam over a greater area and reduce local heating. The cell was heated to 923 K with air flowing over the samples to examine the state of the catalysts at a temperature relevant to CH<sub>4</sub> oxidation. Cubic splines were utilized to remove background fluorescence. Raman peak positions were reproducible to within 1 cm<sup>-1</sup> for strong peaks and 2 cm<sup>-1</sup> for all peaks.

Flow experiments were conducted by supporting the catalyst on a plug of quartz wool in a quartz reactor with a quartz-sheathed thermocouple inserted halfway into the bed

	I					
Catalyst	Mo surface concentration	Specific surface area	Bulk density	Skeletal density	Porosity $\varepsilon$	Residual exposed
	$(Mo nm^{-2})$	$(m^2 g^{-1})$	$(g  cm^{-3})$	$(g  cm^{-3})$		suitace area ζ
$SiO_2$ $MoO_x/SiO_2$	0.44	460 426	0.570 0.660	2.20 2.28	0.741 0.711	1 1.01



Fig. 1. Schematic of reactor configurations utilized. The bulbless configuration was used for most of the experiments. The configuration utilizing a bulb was utilized to gather data at long contact times.

for temperature control. Two reactor geometries were utilized: one with a bulb and one without, depending on how much catalyst was needed. The reactors are shown schematically in Fig. 1. The tubing downstream of the bulb was of smaller diameter (2 mm) so that the product gases would be transported out of the heated zone as rapidly as possible after they left the catalyst bed [7]. The mass of the quartz wool plug was approximately 50 mg. We measured the activity of the quartz wool plug by running the reactor with and without the plug in place. The activity of the plug was undetectable for  $CH_4$  oxidation and reacted with less than 5% of the  $CH_2O$  fed under the slowest flow conditions employed here.

The reactor was heated over a 15-cm zone with a 60-V Omegalux radiant heater (Omega CFRC-16/60-C-A). The vestibules at each end of the heater were stuffed with glass wool insulation. CH<sub>4</sub>, O<sub>2</sub>, and He were delivered to the manifold via Porter 201 mass flow controllers, which were calibrated with a bubble meter. CH<sub>2</sub>O was added to the feed stream by passing on O<sub>2</sub>/He flow through a saturator filled with beads of solid paraformaldehyde (Aldrich; 95% pure). We controlled the CH<sub>2</sub>O vapor pressure in the saturator by recirculating heated water through a jacket surrounding the saturator. The temperature of the water was controlled with a Thermo Electron Neslab RTE-7 recirculating heater/chiller. A temperature of about 331 K was necessary to achieve a vapor pressure of 0.01 atm CH<sub>2</sub>O in the saturator. Typical formaldehyde molar fractions observed during CH<sub>4</sub> oxidation were on the order of 1%, so similar molar fractions were targeted for studies of formaldehyde consumption. The feed flow could be directed through the catalyst bed or through a bypass for analysis of feed composition. All tubing downstream of the saturator was maintained at about 423 K with heat tapes to prevent condensation of water or solid

paraformaldehyde on the tubing walls. Pressure was monitored with a pressure transducer (Omega PX 543-150GI) positioned before the reactor. A National Instruments Lab-View interface was utilized with a Porter PCIM-4 controller to apply composition and total flow program setpoints to the mass flow controllers, and with an Omega CN3251 controller to apply temperature program setpoints to the radiant heater. Contact times were determined taking total pressure and temperature, as well as molar flow rates, into account, since the pressure was as high as  $\sim 2$  atm for the highest flow rates utilized:

$$\tau = \frac{V}{F'} = \left(\frac{m\varepsilon}{\rho_{\rm b}}\right) \bigg/ \bigg(\frac{FRT}{P}\bigg). \tag{4}$$

In this expression,  $\tau$  is the contact time, V is the gas volume within the catalyst bed, F' is the volumetric flow rate, m is the catalyst mass,  $\varepsilon$  is the catalyst porosity,  $\rho_{\rm b}$  is the bulk catalyst density, F is the molar flow rate, R is the gas constant, T is the absolute temperature, and P is the total pressure. This definition differs slightly from the definition of space time, in which the reactor volume is the total volume occupied by the catalyst bed (the factor  $\varepsilon$  is omitted). The contact time defined in this way accurately reflects the amount of time the gas is within the catalyst bed. This detail becomes important when analysing homogeneous rates of reaction within a catalyst bed.

An HP 6890N gas chromatograph with a heated 250-µl sampling loop was used to measure the composition of both the reactor feed and the reactor effluent. A 30-foot-long, 1/8-inch-diameter column packed with Hayesep DB 80/100 mesh was used to separate all components. The column temperature was held at 278 K for 7 min, ramped at 45 K min<sup>-1</sup> to 423 K, and held at 423 K for 15 min. Eluted components were detected with a thermal conductivity detector. Repeated measurements of feed flows demonstrated standard deviations of 2% or less for all feed components relative to mean amounts. CH<sub>2</sub>O peak areas were calibrated in the following manner. A mixture of CH<sub>2</sub>O, O<sub>2</sub>, and He was passed through reactor loaded with 5% Pd/Al<sub>2</sub>O<sub>3</sub>, which combusted CH<sub>2</sub>O completely to CO<sub>2</sub>. The amount of CH<sub>2</sub>O responsible for each CH<sub>2</sub>O peak observed during bypass of the reactor was set equal to the corresponding amount of CO<sub>2</sub> observed after complete combustion.

# 3. Modeling methods

During CH<sub>4</sub> oxidation over MoO<sub>x</sub>/SiO<sub>2</sub>, reactions can occur in the gas phase, on the exposed SiO<sub>2</sub> support, and on the supported MoO<sub>x</sub>. To ascertain the contributions of each of these reactive media to the observed reaction rates, reactions were conducted with an empty reactor and with the reactor filled with either bare SiO<sub>2</sub> or the MoO<sub>x</sub>/SiO<sub>2</sub> catalyst. The overall (observed) rate of reaction is assumed to be the sum of the individual contributions. For reactions over bare SiO<sub>2</sub>, the observed reaction rates are assumed to include the rates in the gas phase and the rates on the SiO<sub>2</sub> surface. For reactions over  $MoO_x/SiO_2$ , the rates include both of these contributions and the contribution of the supported  $MoO_x$ moieties. Denoting homogeneous reaction with H, reaction on the SiO<sub>2</sub> surface with S, and reaction on the supported  $MoO_x$  with M, the observed rates over SiO<sub>2</sub> are thus

$$r_i = \varepsilon r_{i\rm H} + r_{i\rm S} \tag{5}$$

and the rates over  $MoO_x/SiO_2$  are

$$r_i = \varepsilon r_{i\mathrm{H}} + \zeta r_{i\mathrm{S}} + r_{i\mathrm{M}}.\tag{6}$$

In Eqs. (5) and (6), all rates have units of mol cm<sup>-3</sup> s<sup>-1</sup>. Surface reaction rates are normalized by catalyst bed volume to allow summation with the homogeneous reaction rate. The rates are easily converted to the typical area or molar bases by multiplication by the appropriate bulk catalyst properties taken from Table 1:

$$r'_{iS} (\operatorname{mol}_{i} \operatorname{m}^{-2} \operatorname{s}^{-1}) = \frac{r_{iS} (\operatorname{mol}_{i} \operatorname{cm}^{-3} \operatorname{s}^{-1})}{a_{\mathrm{m}}^{0} (\operatorname{m}^{2} \operatorname{g}^{-1}) \times \rho_{\mathrm{b}}^{0} (\operatorname{g} \operatorname{cm}^{-3})},$$
(7)  
$$r''_{iM} (\operatorname{mol}_{i} \operatorname{mol}_{\mathrm{Mo}}^{-1} \operatorname{s}^{-1}) = \left( r_{iM} (\operatorname{mol}_{i} \operatorname{cm}^{-3} \operatorname{s}^{-1}) \times 6.02 \times 10^{23} (\operatorname{Mo} \operatorname{mol}_{\mathrm{Mo}}^{-1}) \right) / \left( a_{\mathrm{m}} (\operatorname{m}^{2} \operatorname{g}^{-1}) \times \rho_{\mathrm{b}} (\operatorname{g} \operatorname{cm}^{-3}) \right)$$

× 10<sup>18</sup> (nm<sup>2</sup> m<sup>-2</sup>) × 
$$c_{\rm Mo}$$
 (Mo nm<sup>-2</sup>)). (8)

In Eqs. (5) and (6) the rate of homogeneous reaction  $r_{i\rm H}$  is reduced by the factor  $\varepsilon$  to account for the fraction of the catalyst bed occupied by the gas phase. The rate of reaction over SiO<sub>2</sub> is assumed to be proportional to the SiO<sub>2</sub> surface area, and hence the rate of reaction over bare SiO<sub>2</sub> is multiplied by  $\zeta$  in Eq. (6) in order to describe the extent to which such reaction contributes to the overall surface reaction occurring on MoO<sub>x</sub>/SiO<sub>2</sub>.

Reaction modeling and data fitting were performed with the use of a plug-flow reactor (PFR) model implemented in Mathematica. The effects of axial dispersion were examined but were found to have very little impact on the values of the extracted kinetic parameters, so an ideal PFR model was utilized. The differential equations describing the concentration profiles of gaseous and surface species were solved along the length of the reactor, with the NDSolve algorithm as a shooting method. The calculated gas-phase composition of the reactor effluent was compared with the experimentally observed effluent composition in terms of the mean observed reaction rate, calculated as

$$\langle r_i \rangle = \frac{Fz_i X_i}{V} = \frac{F(z_i - y_i)}{V},\tag{9}$$

where  $X_i$ ,  $y_i$ , and  $z_i$  are, respectively, the conversion, effluent fraction, and feed fraction of component *i*. For homogeneous reaction, *V* is the reactor volume. For reaction over a solid catalyst, *V* is the volume of the catalyst bed,  $m/\rho_b$ . Rates reported here are mean rates calculated according to Eq. (9) unless otherwise noted. We minimized the sum of the

squared differences between the mean rates observed experimentally and calculated from the model by adjusting kinetic parameters with the FindMinimum search algorithm.

During CH<sub>4</sub> oxidation, O<sub>2</sub> was the limiting reagent. The O<sub>2</sub> conversion varied from 1% to as high as 95%, depending on operating conditions. During CH<sub>2</sub>O oxidation/decomposition, CH<sub>2</sub>O was the limiting reagent, and CH<sub>2</sub>O conversions approached  $\sim$  75% in some cases. Because a plug-flow reactor model was used, and because the state of the surface is taken into account in the model, high reactant conversions do not present a problem in the analysis of the rate data.

### 4. Results and discussion

#### 4.1. Catalyst characterization

The Raman spectra of the bare SiO<sub>2</sub> support under ambient conditions and at 923 K under flowing air are shown in Fig. 2. The spectra show features characteristic of the tetrahedral SiO<sub>2</sub> network at 430, 805, 1060, and 1180 cm<sup>-1</sup>. The bands at 605 and 490 cm<sup>-1</sup> are assigned to the D<sub>1</sub> and D<sub>2</sub> defect features, respectively, and the band at 970 cm<sup>-1</sup> is assigned to the Si–O stretching vibrations of silanol groups [18–20]. The spectrum of the bare SiO<sub>2</sub> does not change upon heating to 923 K in flowing air, but the Raman scattering amplitude increases by about tenfold.

Raman spectra for the  $MoO_x/SiO_2$  catalyst at ambient temperature and at 923 K are shown in Fig. 3. Under ambient conditions, the spectrum shows features at 870 and 955 cm<sup>-1</sup> that are indicative of surface polymolybdate species [21,22]. Upon heating in dry flowing air to 923 K, the polymolybdate species disperse to yield isolated monooxo molybdate species, characterized by the single Mo=O



Fig. 2. Raman spectra of bare  $SiO_2$  (a) under ambient conditions and (b) at 923 K under flowing air. Ambient spectrum amplified  $10 \times$ .



Fig. 3. Raman spectra of  $MoO_x/SiO_2$  (a) under ambient conditions and (b) at 923 K under flowing air. Ambient spectrum amplified 5×.

stretching frequency observed at 985 cm<sup>-1</sup> [22-28]. The SiO<sub>2</sub> features at 430, 490, 605, 805, and 1190 cm<sup>-1</sup> are all clearly observed, but the features at 975 and 1060  $cm^{-1}$  are obscured by the intense Mo=O stretching band. The feature at 370 cm<sup>-1</sup> in the spectra of the MoO<sub>x</sub>/SiO<sub>2</sub> under ambient conditions and at 923 K has been assigned as the bending mode of surface molybdate species [22]. The spectra observed under ambient conditions and during heating at 923 K are similar to those previously observed for  $MoO_x/SiO_2$  prepared by deposition-precipitation [23]. The similarity of the Raman spectra is consistent with previous findings that the structure of SiO<sub>2</sub>-supported  $MoO_x$  moieties is independent of the Mo precursor after high-temperature calcination [21]. Raman spectra similar to that shown in Fig. 3 have been recorded during CH<sub>4</sub> oxidation at 823 K [22,24,25], suggesting that supported  $MoO_x$  does not restructure under conditions of CH<sub>4</sub> oxidation.

The coordination of  $MoO_x/SiO_2$  at these low weight loadings is octahedral under ambient conditions [21], but the structure under dehydrated conditions has been disputed in the literature, with some authors claiming tetrahedral coordination [26,27], others claiming distorted octahedral coordination [24,25,29,30], and some claiming a geometry "intermediate" between tetrahedral and octahedral [31]. The broad bands observed by UV-visible spectroscopy for this catalyst and the close proximity of the ligand-to-metal charge transfer bands for the T<sub>d</sub> and O<sub>h</sub> coordination preclude the use of the technique as a definitive indicator of coordination [29,32]. The most useful method for determining Mo coordination in this case is XANES. LIII-edge XANES data for  $MoO_x/SiO_2$  suggest a degree of non-centrosymmetry for Mo intermediate between  $O_h$  and  $T_d$  [31]. Based on this observation and the observation by Raman and IR that the  $MoO_x/SiO_2$  has a single terminal oxo group, it seems likely that the SiO<sub>2</sub>-supported  $MoO_x$  moieties observed at 923 K



Fig. 4. Carbon selectivity versus methane conversion for methane oxidation over bare SiO<sub>2</sub> at 873 K. Feed composition is 90% CH<sub>4</sub>, 10% O<sub>2</sub>. CH<sub>4</sub> conversion was varied by varying contact time. Trendlines are empirical polynomial fits.



Fig. 5. Carbon selectivity versus methane conversion for methane oxidation over  $0.44 \text{ Mo nm}^{-2} \text{ MoO}_x/\text{SiO}_2$  at 873 K. Feed composition is 90% CH<sub>4</sub>, 10% O<sub>2</sub>. CH<sub>4</sub> conversion was varied by varying contact time. Trendlines are empirical polynomial fits.

are pentacoordinate. A trigonal bipyramid or square pyramid will have a degree of non-centrosymmetry intermediate between  $O_h$  and  $T_d$  and will have six total bonds with a single terminal oxo group. Such a coordination has previously been assigned to  $MoO_x/ZrO_2$  at low loadings after calcination at 973 K, based on Raman spectroscopic observations [33].

# 4.2. Product distribution

The product distributions observed during CH<sub>4</sub> oxidation at 873 K over bare SiO<sub>2</sub> and over MoO<sub>x</sub>/SiO<sub>2</sub> are plotted versus CH<sub>4</sub> conversion in Figs. 4 and 5, respectively. Over both catalysts the product distribution approaches 100% CH<sub>2</sub>O as the CH<sub>4</sub> conversion approaches zero, demonstrating that CH<sub>2</sub>O is the only initial product. As the CH<sub>4</sub> conversion increases, the CH<sub>2</sub>O selectivity decreases and the selectivities for CO and CO<sub>2</sub> increase. These results demonstrate that CO<sub>x</sub> is produced in secondary reactions from CH<sub>2</sub>O.

Whereas several authors have also made observations indicating that the initial product distribution of CH<sub>4</sub> oxidation over  $MoO_x/SiO_2$  is > 95% CH<sub>2</sub>O [7,34–36], Spencer and Pereira reported a product distribution of 89% CH<sub>2</sub>O and 11% CO<sub>2</sub> in the limit of zero CH<sub>4</sub> conversion [37]. A possible explanation for this discrepancy is the presence of CO<sub>2</sub> in the CH<sub>4</sub> supply. At very low CH<sub>4</sub> conversion, the concentration of CO<sub>2</sub> contaminant becomes comparable to the concentrations of reaction products, and the apparent initial product distribution will include this contaminant CO<sub>2</sub> if it is uncorrected.

Based on our observations of the change in product distribution with  $CH_4$  conversion, we assume that  $CH_4$  is oxidized selectively to  $CH_2O$ , and that  $CO_x$  (CO and  $CO_2$ ) is formed solely from subsequent reaction of  $CH_2O$ :

$$CH_4 \rightarrow CH_2O \rightarrow CO_x$$

Exclusion of a direct pathway from  $CH_4$  to  $CO_2$  allows CO and  $CO_2$  to be treated as a single product ( $CO_x$ ) in the analysis of the kinetics of  $CH_2O$  formation and consumption.

The ratio of CO/CO<sub>2</sub> observed during CH<sub>2</sub>O oxidation/decomposition was about 12 over bare SiO<sub>2</sub> and about 9 over MoO<sub>x</sub>/SiO<sub>2</sub>. During CH<sub>4</sub> oxidation, the ratio was in the range of 8–10 over bare SiO<sub>2</sub> and 5.5–7 over MoO<sub>x</sub>/SiO<sub>2</sub>. The lower ratios observed during CH<sub>4</sub> oxidation are probably due to the higher partial pressure of H<sub>2</sub>O during CH<sub>4</sub> oxidation and the water–gas shift equilibrium reaction, which lies toward CO<sub>2</sub> under the operating conditions employed in this study. Since the interconversion of CO and CO<sub>2</sub> was not investigated, no attempt was made to include the effects of this process in the modeling of CH<sub>2</sub>O formation and consumption.

#### 4.3. Methane oxidation

Homogeneous oxidation of CH<sub>4</sub> is not measurable under the conditions employed in this study. Whereas Baldwin et al. have found that homogeneous oxidation of CH<sub>4</sub> by O<sub>2</sub> becomes measurable at 923 K for residence times greater than 2 s and pressures greater than 2 atm [9], the contact times employed for CH<sub>4</sub> oxidation over MoO<sub>x</sub>/SiO<sub>2</sub> are typically less than 1 s, and the pressures are typically less than 2 atm. Therefore only the contributions of the bare SiO<sub>2</sub> and supported MoO<sub>x</sub> are considered in the modeling of CH<sub>4</sub> oxidation.

The kinetics of  $CH_4$  oxidation over bare  $SiO_2$  have been successfully described by Arena et al. with the use of a twosite, dissociative mechanism allowing for surface oxygen vacancies [10]. The model successfully described the extent of catalyst reduction observed by pulse  $O_2$  chemisorption. The two-site dissociative mechanism includes the following reactions:

$$CH_4 + 2MO \rightarrow CH_2O + H_2O + 2M, \tag{1S}$$

$$CH_{2}O + \left(\frac{S_{CO} + 2S_{CO_{2}}}{S_{CO} + S_{CO_{2}}}\right)MO$$
  

$$\rightarrow CO_{x} + H_{2}O + \left(\frac{S_{CO} + 2S_{CO_{2}}}{S_{CO} + S_{CO_{2}}}\right)M,$$
(2S)

$$2M + O_2 \rightarrow 2MO. \tag{3S}$$

In these equations, MO represents an oxidized surface site and M a reduced surface site. The factor  $n_S$  is the moles of O<sub>2</sub> consumed per mole of CH<sub>4</sub> consumed. Oxidized and reduced active sites are taken to be the only surface species present and are thus conserved according to

$$\theta_{\rm ox} + \theta_{\rm red} = 1. \tag{10}$$

In Eq. (10),  $\theta_{ox}$  is the fraction of active sites in the oxidized form (MO) and  $\theta_{red}$  is the fraction of active sites in the reduced form (M).

The rates of reactions (1S) and (2S) are written as

$$r_{1\rm S} = k_{1\rm S} \, p_{\rm CH_4} \theta_{\rm ox}^2,\tag{11}$$

$$r_{3S} = k_{3S} p_{O_2} \theta_{\text{red}}^2 = k_{3S} p_{O_2} (1 - \theta_{\text{ox}})^2,$$
(12)

where  $r_{iS}$  is the reaction rate of reaction *i* on the SiO<sub>2</sub> surface,  $k_i$  is the corresponding rate constant, and  $p_j$  is the partial pressure of component *j*. We determined the fraction of the surface sites oxidized under given conditions  $\theta_{ox}$  by equating the rates of surface reduction and oxidation at steady state:

$$n_{\rm S}r_{\rm 1S} = r_{\rm 3S}.$$
 (13)

The rate laws in Eqs. (11) and (12) are substituted into Eq. (13) and solved for  $\theta_{ox}$  in terms of rate constants, partial pressures of CH<sub>4</sub> and O<sub>2</sub>, and  $n_s$ . According to this kinetic scheme,  $\theta_{ox}$  depends only on the ratio of partial pressures of CH<sub>4</sub> and O<sub>2</sub> [10].

If it is assumed that CO and CO<sub>2</sub> are formed exclusively by the reactions

$$CH_2O + MO \rightarrow CO + H_2O + M$$
,

$$CH_2O + 2MO \rightarrow CO_2 + H_2O + 2M$$

then  $n_{\rm S}$  is related to the product distribution by

$$n_{\rm S} = S_{\rm CH_2O} + 1.5S_{\rm CO} + 2S_{\rm CO_2}.$$
 (14)

Therefore,  $n_S$  is 1 for a product distribution of 100% CH<sub>2</sub>O and 1.5 for 100% CO. Arena et al. demonstrated that  $\theta_{ox}$  is insensitive to  $n_S$  and used  $n_S = 1.25$ , based on an approximate product distribution of 50% CH<sub>2</sub>O, 50% CO. We observed a value of  $n_S \approx 1.18$  for CH<sub>4</sub> oxidation over SiO<sub>2</sub> for the range of CH<sub>4</sub> conversions over which rate data were fit. However, as discussed below, the reaction of CH<sub>2</sub>O over SiO<sub>2</sub> does not appear to consume oxygen, and hence we took  $n_S = 1$  in Eq. (13).

Rate data for the oxidation of CH<sub>4</sub> over bare SiO<sub>2</sub> at 873 K are shown in Fig. 6. We increased the CH<sub>4</sub>/O<sub>2</sub> feed ratio from 1.6 to 7.5 by increasing the feed fraction of CH<sub>4</sub> from 19 to 87% while holding the O<sub>2</sub> feed fraction constant at 13% (the balance was He). We further increased the CH<sub>4</sub>/O<sub>2</sub> feed ratio to 22.7 by decreasing the O<sub>2</sub> feed fraction. The CH<sub>4</sub> oxidation rate exhibits a maximum at CH<sub>4</sub>/O<sub>2</sub> = 7.5, where both reactants are at their maximum values. The model represented by Eqs. (10)–(13) was fit to the data by adjustment of the values of  $k_{1S}$ 



Fig. 6. Rate of CH<sub>4</sub> oxidation versus CH<sub>4</sub>:O<sub>2</sub> ratio over bare SiO<sub>2</sub>. CH<sub>4</sub> feed fraction was increased from 19 to 87% at 13% O<sub>2</sub> (balance He). CH<sub>4</sub> feed fraction was then held constant at 87% while O<sub>2</sub> feed fraction was reduced to 3.3% (balance He). Data recorded at 873 K with 0.65 s contact time. Model fit by varying  $k_{1S}$  and  $k_{3S}$ .



Fig. 7. Rate of CH<sub>4</sub> oxidation over bare SiO<sub>2</sub> versus temperature. Data recorded with 0.65 s contact time and feed composition of 87% CH<sub>4</sub>, 13% O<sub>2</sub>. Model fit by varying  $E_{1S}$  and  $E_{4S}$ .

and  $k_{4S}$ . As shown in Fig. 6, the model satisfactorily describes the CH<sub>4</sub> oxidation rate with respect to both reactants. Values of  $k_{1S}$  and  $k_{3S}$  at 873 K were found to be 0.122 and 50.3 µmol cm<sup>-3</sup> atm<sup>-1</sup> s<sup>-1</sup>, respectively (0.466 and 192 nmol m<sup>-2</sup> atm<sup>-1</sup> s<sup>-1</sup> when normalized by surface area). The ratio of the rate constants  $k_{1S}/k_{3S}$  is 0.0024, which is about 50% higher than the value of 0.00159 reported by Arena et al. [10] at 873 K. The temperature dependence of the CH<sub>4</sub> oxidation rate over bare SiO<sub>2</sub> is shown in Fig. 7. The two-site dissociative mechanism is fit to data with the assumption of Arrhenius forms for the rate constants  $k_{1S}$  and  $k_{3S}$ . A good fit to the data is obtained with values for the activation energies of  $E_{1S} = 152$  kJ mol<sup>-1</sup> and  $E_{3S} = 0$ . These values of  $E_{1S}$  and  $E_{3S}$  are in reasonable agreement with the findings of Arena et al., who reported activation energies of 159 and 20 kJ mol<sup>-1</sup> for the respective reactions.

The speciation of the active sites on  $SiO_2$  is plotted versus the  $CH_4/O_2$  ratio at 923 K in Fig. 8. With the model formu-



Fig. 8. SiO<sub>2</sub> surface state predicted by model versus CH<sub>4</sub>:O<sub>2</sub> ratio at 923 K.



Fig. 9. Rate of CH<sub>4</sub> oxidation versus CH<sub>4</sub>:O<sub>2</sub> ratio over MoO<sub>x</sub>/SiO<sub>2</sub>. CH<sub>4</sub> feed fraction was increased from 20 to 90% at 10% O<sub>2</sub> (balance He). CH<sub>4</sub> feed fraction was then held constant at 90% while O<sub>2</sub> feed fraction was reduced to 2.7% (balance He). Data recorded at 873 K at 0.85 s contact time. Dashed line shows model treating kinetics over MoO<sub>x</sub> with rate laws of the same form as those used for bare SiO<sub>2</sub>. Solid line shows model accounting for surface carbonaceous species.

lated as described above, the speciation of active sites on the  $SiO_2$  surface is completely specified by the  $CH_4/O_2$  ratio. The fraction of oxidized sites predicted by the kinetic model falls from 88% at a  $CH_4/O_2$  ratio of 2 to 67% at a  $CH_4/O_2$ ratio of 33. Since the rate of CH<sub>4</sub> oxidation is proportional to the square of the fraction of oxidized sites, the rate of CH<sub>4</sub> oxidation decreases by 42%. The agreement between our model derived from kinetic observations and the pulse  $O_2$  chemisorption observations of Arena et al. is quite good, but our model predicts a slightly more reduced surface over the range of  $CH_4/O_2$  ratios for which data were available. At a CH<sub>4</sub>/O<sub>2</sub> ratio of 8, our kinetic model predicts 20% surface vacancies, whereas O2 chemisorption data reported by Arena et al. demonstrate 17% vacancies [10]. This small discrepancy could be ascribed to the different sources of SiO2 in the two studies.

The rate of CH<sub>4</sub> oxidation over  $MoO_x/SiO_2$  at 873 K is plotted versus the CH<sub>4</sub>/O<sub>2</sub> ratio in Fig. 9. The exper-

imental conditions are the same as those employed in the experiments conducted over bare SiO<sub>2</sub> shown in Fig. 6. The CH<sub>4</sub> feed fraction is increased to raise the CH<sub>4</sub>/O<sub>2</sub> feed ratio from 2 to 9, and we further raised the feed ratio by decreasing the O<sub>2</sub> feed fraction. The dashed line shows the best fit to the CH<sub>4</sub> oxidation rate data of a model formulated with the assumption that the rate laws for the reactions occurring on the supported MoO<sub>x</sub> are of exactly the same form as those occurring on the SiO<sub>2</sub> surface (Eqs. (10)–(13)). It is evident that the two-site dissociative mechanism describing the SiO<sub>2</sub> surface is incapable of properly describing the kinetics occurring on the supported MoO<sub>x</sub>. Although the general shape of the rate dependence is correct, the sensitivity of the rate to both the CH<sub>4</sub> and the O<sub>2</sub> partial pressures is too high.

To correctly model the kinetics occurring over the SiO<sub>2</sub>supported MoO<sub>x</sub>, the mechanism assumed for SiO<sub>2</sub> must be modified to include another kinetically relevant surface species. This can be done by assuming that CH<sub>2</sub>O is formed in a two-step process. The CH<sub>4</sub> is assumed to adsorb dissociatively and reversibly to yield methoxide species, which are then oxidized to yield CH<sub>2</sub>O:

$$CH_4 + MO \rightleftharpoons MOCH_3 + H_S,$$
 (0M)

$$MOCH_3 + MO \rightarrow CH_2O + M + MOH.$$
 (1M)

The oxidation of  $CH_2O$  over supported  $MoO_x$  and the reoxidation of  $MoO_x$  sites are assumed to occur via the following reactions:

$$CH_{2}O + \left(\frac{S_{CO} + 2S_{CO_{2}}}{S_{CO} + S_{CO_{2}}}\right)MO$$
  

$$\rightarrow CO_{x} + H_{2}O + \left(\frac{S_{CO} + 2S_{CO_{2}}}{S_{CO} + S_{CO_{2}}}\right)M,$$
(2M)

$$2M + O_2 \rightarrow 2MO. \tag{3M}$$

The factor  $n_{\rm M}$  is the ratio of the moles of O<sub>2</sub> consumed per mole of CH<sub>4</sub> consumed on the supported MoO<sub>x</sub> moieties. The hydrogen atom formed in reaction (0M) is assumed to be bonded to the oxygen of a cleaved Mo–O–Si bond. This surface hydrogen is assumed to react rapidly with MOH formed from the oxidation of surface methoxide in reaction (1M) to release H<sub>2</sub>O:

$$H_S + MOH \rightarrow H_2O + M.$$
 (4M)

The surface-catalyzed oxidation of CH<sub>4</sub> to CH<sub>2</sub>O and H<sub>2</sub>O requires a four-electron reduction of the catalyst. Although the MoO<sub>x</sub> sites of MoO<sub>x</sub>/SiO<sub>2</sub> appear to be isolated as discussed above, the mechanism is written to include two molybdenum centers because MoO<sub>x</sub> undergoes a twoelectron reduction from Mo<sup>VI</sup> to Mo<sup>IV</sup> under reducing conditions at temperatures relevant to CH<sub>4</sub> oxidation [26], and hence two MoO<sub>x</sub> centers are required to accommodate the oxidation of CH<sub>4</sub> to CH<sub>2</sub>O. While spectroscopic observations indicate that the MoO<sub>x</sub> moieties do not share bridging oxo groups, these species remain in relatively close proximity after their formation from polymolybdate species. The so-called microspreading of the polymolybdate present on the hydrated catalyst precursor to yield isolated  $MoO_x$  is believed to be a short-range phenomenon [23]. It has been demonstrated that  $MoO_3$  does not spread over macroscopic distances on SiO<sub>2</sub> [38] and that polymolybdate is regenerated upon exposure of isolated  $MoO_x/SiO_2$  to hydrating conditions [22], suggesting a close proximity of isolated  $MoO_x$  moieties. Methoxide was chosen as the most reasonable intermediate because it has been observed upon adsorption of CH<sub>4</sub> at low temperatures over  $MoO_x/SiO_2$  by IR spectroscopy [39].

The rate laws for the reactions occurring on supported  $MoO_x$  are written as

$$r_{\rm 0M} = k_{\rm 0Mf} p_{\rm CH_4} \phi_{\rm ox} - k_{\rm 0Mr} \phi_{\rm C}^2, \tag{15}$$

$$r_{1\mathrm{M}} = k_{1\mathrm{M}}\phi_{\mathrm{C}}\phi_{\mathrm{ox}},\tag{16}$$

$$r_{\rm 3M} = k_{\rm 3M} p_{\rm O_2} \phi_{\rm red}^2, \tag{17}$$

where  $\phi_{ox}$ ,  $\phi_{C}$ , and  $\phi_{red}$  are the fractions of MoO<sub>x</sub> present as oxidized sites (MO), sites with adsorbed methoxide (MOCH<sub>3</sub>), and vacant sites (M), respectively. The subscripts f and r in Eq. (15) denote the forward and reverse rate constants for the dissociative adsorption of CH<sub>4</sub>. The secondorder dependence of the reverse reaction on  $\phi_{\rm C}$  arises because the amount of surface hydrogen H<sub>S</sub> is approximately equal to the amount of MOCH<sub>3</sub>. Surface hydrogen is formed and consumed by adsorption and desorption of CH<sub>4</sub> at the same rates as MOCH<sub>3</sub>. Assuming that reaction (4M) occurs rapidly, then as soon as MOH is formed by oxidation of methoxide, surface hydrogen is consumed to yield H<sub>2</sub>O. Hence, the amount of surface hydrogen is approximately equal to the amount of methoxide, and the reverse rate of the dissociative adsorption is described as an elementary process that is second-order in  $\phi_{\rm C}^2$  (see Eq. (15)).

To solve for  $\phi_{ox}$ ,  $\phi_{red}$ , and  $\phi_C$ , it is necessary to write three steady-state balances for surface species. Balances on MO, MOCH<sub>3</sub>, and total sites provide the necessary equations:

$$2r_{\rm 3M} - r_{\rm 0Mf} + r_{\rm 0Mr} - (n_{\rm M} - 1)r_{\rm 1M} - (n_{\rm S} - 1)\zeta r_{\rm 1S} = 0,$$
(18)

$$r_{0Mf} - r_{0Mr} - r_{1M} = 0,$$
 (19)

$$\phi_{\rm ox} + \phi_{\rm red} + \phi_{\rm C} = 1. \tag{20}$$

The quantity  $-(n_S - 1)\zeta r_{1S}$  is included in the balance on MO (Eq. (18)) because H<sub>2</sub> resulting from non-oxidative decomposition of CH<sub>2</sub>O over the SiO<sub>2</sub> surface is oxidized to H<sub>2</sub>O by MO (see below). Here  $n_S$  is calculated from the observed product distribution during CH<sub>4</sub> oxidation over bare SiO<sub>2</sub> (rather than using  $n_S = 1$  as in Eq. (13)), and  $n_M$  is approximated from the observed product distribution during CH<sub>4</sub> oxidation over MoO<sub>x</sub>/SiO<sub>2</sub>, in the same way as  $n_S$  is in Eq. (14). Although  $n_M$  is not strictly specified as  $n_S$  is in Eq. (14), since it accounts only for the reactions occurring over the supported MoO<sub>x</sub>, Eq. (14) provides a good approximation of  $n_M$  because the majority of CH<sub>4</sub> oxidation occurs on supported MoO<sub>x</sub> and the product distributions over SiO<sub>2</sub> and MoO<sub>x</sub>/SiO<sub>2</sub> are similar. The values of  $n_S$  and  $n_M$  are not



Fig. 10. Arrhenius plots of rate constants  $k_{0Mf}$ ,  $k_{0Mr}$ ,  $k_{1M}$ , and  $k_{3M}$  describing CH<sub>4</sub> oxidation over supported MoO<sub>x</sub>. Data recorded with feed composition of 90% CH<sub>4</sub>, 10% O<sub>2</sub> at 0.38 or 0.24 s contact time.

constant over the length of the reactor but are taken as constants because they vary only slightly and the kinetic model is insensitive to their values. For the small conversion levels at which these expressions were fit to experimental data, the values of  $n_{\rm S}$  and  $n_{\rm M}$  were taken as 1.18 and 1.24, respectively.

From a fit of the model to the data shown in Fig. 9, the values of the rate constants  $k_{0Mf}$ ,  $k_{0Mr}$ ,  $k_{1M}$ , and  $k_{3M}$  at 873 K were determined to be 1.35  $\mu$ mol cm<sup>-3</sup> atm<sup>-1</sup> s<sup>-1</sup>, 710  $\mu$ mol cm<sup>-3</sup> s<sup>-1</sup>, 40.6  $\mu$ mol cm<sup>-3</sup> s<sup>-1</sup>, and 178  $\mu$ mol  $cm^{-3} atm^{-1} s^{-1}$ , respectively. In order to calculate activation energies, we collected data similar to those shown in Fig. 9 at 848, 898, and 923 K. Values of the four rate constants were determined for each temperature; the values obtained are plotted in Fig. 10. Good linearity is observed for temperatures greater than 848 K. At 848 K the rates of reaction are relatively low, and the model begins to deviate from observations. The activation energies for the forward and reverse dissociative adsorption of  $CH_4$ ,  $E_{0Mf}$  and  $E_{0Mr}$ , were found to be 206 and 299 kJ mol<sup>-1</sup>, respectively, indicating an enthalpy loss of 93 kJ mol<sup>-1</sup> upon dissociative adsorption of CH<sub>4</sub>. The activation energy for oxidation of the surface methoxide species was found to be  $269 \text{ kJ mol}^{-1}$ . The rate of surface re-oxidation was practically unaffected by changes in temperature, and correspondingly  $E_{3M}$  is only  $22.2 \text{ kJ mol}^{-1}$ .

The fit of the model to the data is shown in Fig. 11 for temperatures between 848 and 923 K. The sensitivity of the rate of CH<sub>4</sub> oxidation to decreased oxygen partial pressure at high CH<sub>4</sub>/O<sub>2</sub> ratios becomes greater at higher temperature. This is due in part to the greater decrease in O<sub>2</sub> partial pressure along the length of the reactor at higher rates, but is also due to the non-activated nature of the surface re-oxidation (reaction (3M)). The relatively large activation energies for



Fig. 11. Rate of CH<sub>4</sub> oxidation versus CH<sub>4</sub>:O<sub>2</sub> ratio at temperatures of 848, 873, 898, and 923 K. Symbols are data; lines are model predictions using kinetic parameters extracted in Fig. 10. CH<sub>4</sub> feed fraction was increased from 20 to 90% at 10% O<sub>2</sub> (balance He). CH<sub>4</sub> feed fraction was then held constant at 90% while O<sub>2</sub> feed fraction was reduced to 3.3% (balance He). Data recorded at 0.38 s contact time at 848 and 873 K, and at 0.24 s contact time at 898 and 923 K.



Fig. 12. Model predictions of  $MoO_x$  site speciation versus  $CH_4:O_2$  ratio during  $CH_4$  oxidation at 873 K.  $CH_4$  feed fraction increased from 0 to 90% while holding  $O_2$  feed fraction constant at 10%, then  $O_2$  feed fraction decreased from 10 to 2.5% while holding  $CH_4$  feed fraction constant at 90% (balance He). Percentage of surface carbonaceous species amplified 10 times.

the reactions of CH<sub>4</sub> cause the rates of surface reduction to increase sharply with temperature, whereas the rate of surface re-oxidation does not increase appreciably with temperature. As a result, more surface vacancies are present at higher temperature for a given gas-phase composition. The speciation of MoO<sub>x</sub> sites predicted by the kinetic model is shown in Fig. 12 versus gas composition at 873 K. Increasing the gas-phase fraction of CH<sub>4</sub> from 20 to 90% at 10% O<sub>2</sub> increases the fraction of MoO<sub>x</sub> with oxygen vacancies from 12 to 20% and increases the fraction of MoO<sub>x</sub> with adsorbed methoxide from 0.8 to 2.5%. Decreasing the gasphase O<sub>2</sub> fraction from 10 to 2.5% at 90% CH<sub>4</sub> results in a further increase of the fraction of vacancies to 34%. The fraction of MoO<sub>x</sub> containing adsorbed methoxide species



Fig. 13. Extraction of kinetic orders  $\alpha$  and  $\beta$  of the homogeneous CH<sub>2</sub>O reaction. (\*) varying CH<sub>2</sub>O at 11% O<sub>2</sub> feed fraction and (---) linear fit with slope of 2.55; (**A**) varying O<sub>2</sub> feed fraction at 1.1% CH<sub>2</sub>O feed fraction and (—) linear fit with slope of 0.61. Conversion of CH<sub>2</sub>O was less than 20% throughout; conversion of O<sub>2</sub> was less than 2%. Recorded at 873 K, 1.62 atm absolute total pressure, and 0.9 s residence time.

decreases slightly to 2.4%, as fewer oxidized sites are available for dissociative adsorption of CH<sub>4</sub>. Thus, the fraction of MoO<sub>x</sub> sites available for CH<sub>4</sub> oxidation (oxidized sites) decreases with increasing CH<sub>4</sub> partial pressure or decreasing O<sub>2</sub> partial pressure. This is manifested in the observed negative curvature of the CH<sub>4</sub> oxidation rate with increased CH<sub>4</sub> feed fraction and in the decreased CH<sub>4</sub> oxidation rate with decreased O<sub>2</sub> feed fraction.

# 4.4. Reactions of formaldehyde

The reaction of CH<sub>2</sub>O over bare silica or supported  $MoO_x/SiO_2$  has not received nearly the attention dedicated to the oxidation of CH<sub>4</sub> over the same catalysts, and hence the rate laws for the reaction of CH<sub>2</sub>O are not as well known as those for CH<sub>4</sub> oxidation. Useful information regarding the rate laws was obtained from reaction of CH<sub>2</sub>O/O<sub>2</sub>/He mixtures over these catalysts at temperatures relevant to CH<sub>4</sub> oxidation. The homogeneous reaction of CH<sub>2</sub>O was also investigated under the same reaction conditions to determine its relative importance during oxidation over the solid catalysts.

The homogeneous reaction of CH<sub>2</sub>O produces  $CO_x$ , typically with a carbon selectivity of > 90% CO and < 10% CO<sub>2</sub>. The homogeneous reaction proceeds via a radical network [8] and was modeled by a fit of rate data to an empirical rate law:

$$r_{\rm 2H} = k_{\rm 2H} p^{\alpha}_{\rm CH_2O} p^{\beta}_{\rm O_2}.$$
 (21)

Fig. 13 shows rate data for homogeneous CH<sub>2</sub>O reaction versus the mean CH<sub>2</sub>O and O<sub>2</sub> molar fractions. The kinetic orders were extracted from the log–log plot shown rather than by use of a PFR model because the data showed good linearity on the log–log plot, and the additional precision afforded by the PFR model was deemed unnecessary. The data are well represented by Eq. (21) with  $\alpha = 2.55$ ,  $\beta = 0.61$ , and  $k_{2H} = 5.2 \times 10^{-3} \text{ mol cm}^{-3} \text{ atm}^{-3.16} \text{ s}^{-1}$ .



Fig. 14. Arrhenius plot of homogeneous  $CH_2O$  reaction rate. Feed composed of 1.1%  $CH_2O$ , 11%  $O_2$ , balance He at 1.62 atm absolute total pressure, 0.9 s residence time.



Fig. 15. Extraction of kinetic orders of CH<sub>2</sub>O reaction with respect to CH<sub>2</sub>O over bare SiO<sub>2</sub> and MoO<sub>x</sub>/SiO<sub>2</sub>. Varying CH<sub>2</sub>O feed fraction at 11% O<sub>2</sub>, balance He at 873 K. (•) Data recorded over bare SiO<sub>2</sub> and (—) linear fit with slope of 0.93; (**■**) data recorded over MoO<sub>x</sub>/SiO<sub>2</sub> and (---) linear fit with slope of 0.98.

The large value of  $\alpha$  is consistent with the observation of increased CH<sub>2</sub>O conversion with increased CH<sub>2</sub>O partial pressure made by Baldwin et al. [9]. The large exponent is attributable to the multiple roles of CH<sub>2</sub>O and its fragments in the CH<sub>2</sub>O reaction network. An Arrhenius plot of  $k_{2H}$  versus temperature for temperatures of 848 K to 923 K is shown as Fig. 14. The activation energy determined from the slope of this plot is 231 kJ mol<sup>-1</sup>. This is higher than the values of 96 to 109 kJ mol<sup>-1</sup> reported by other workers at temperatures of 573 to 823 K, but is comparable to the value of 209 kJ mol<sup>-1</sup> reported for reaction vessels coated with "oxidation inhibitors" to suppress reactions occurring on the vessel walls [8].

Fig. 15 shows the dependence of the rate of CH<sub>2</sub>O consumption at 873 K on the CH<sub>2</sub>O feed fraction for reaction over bare SiO<sub>2</sub> and over MoO<sub>x</sub>/SiO<sub>2</sub>. The reaction obeys



Fig. 16. Rate of CH<sub>2</sub>O consumption versus O<sub>2</sub> feed fraction at 873 K with 1.1% CH<sub>2</sub>O feed fraction. (•) Data recorded over bare SiO<sub>2</sub> and (—) model fit by varying  $k_{2S}$ ; (**1**) data recorded over MoO<sub>x</sub>/SiO<sub>2</sub> and (---) model fit by varying  $k_{2M}^{(0)}$  and  $k_{2M}^{(1)}$ .

Table 2 Mean rates of CH<sub>2</sub>O reaction at 873 K with 1.1% CH<sub>2</sub>O feed fraction

Catalyst	$r_{\rm CH_2O}$ (µmol cm <sup>-</sup>	$r_{\rm CH_2O} \ (\mu {\rm mol}  {\rm cm}^{-3}  {\rm s}^{-1})$		
	11% O <sub>2</sub>	No O <sub>2</sub>		
Empty tube	0.043	0.005		
SiO <sub>2</sub>	0.20	0.19		
$MoO_x/SiO_2$	0.95	0.49		

first-order kinetics with respect to  $CH_2O$  over both  $SiO_2$ and  $MoO_x/SiO_2$ , so linear regression of log–log data of the  $CH_2O$  consumption rate versus  $CH_2O$  feed fraction yields a slope of very nearly 1 in both cases.

The rate of CH<sub>2</sub>O consumption at 873 K over bare SiO<sub>2</sub> and over  $MoO_x/SiO_2$  is shown in Fig. 16 as a function of the fraction of O<sub>2</sub> in the feed. With no O<sub>2</sub> in the feed, CO and H<sub>2</sub> are produced in equivalent quantities, consistent with the pyrolytic decomposition of CH<sub>2</sub>O:

 $CH_2O \rightarrow CO + H_2.$ 

When bare SiO<sub>2</sub> is used as the catalyst, the rate of CH<sub>2</sub>O consumption increases very slightly with increasing O<sub>2</sub> feed fraction, and only a small fraction (~ 20%) of the H<sub>2</sub> generated is oxidized. The decomposition of CH<sub>2</sub>O also occurs over the MoO<sub>x</sub> moieties, as indicated by the increase in the rate of CH<sub>2</sub>O decomposition in the absence of O<sub>2</sub> over MoO<sub>x</sub>/SiO<sub>2</sub> (0.49 µmol cm<sup>-3</sup> s<sup>-1</sup> relative to the rate over bare SiO<sub>2</sub> (0.19 µmol cm<sup>-3</sup> s<sup>-1</sup>). As O<sub>2</sub> is added to the feed, the rate of CH<sub>2</sub>O consumption over MoO<sub>x</sub>/SiO<sub>2</sub> increases by almost a factor of 2 to 0.95 µmol cm<sup>-3</sup> s<sup>-1</sup>, and all H<sub>2</sub> formed is combusted to H<sub>2</sub>O. In separate experiments in which H<sub>2</sub>/O<sub>2</sub> mixtures were fed to the reactor, it was confirmed that the rate of H<sub>2</sub> combustion was very small over bare SiO<sub>2</sub> but comparable to the rate of cH<sub>2</sub>O over MoO<sub>x</sub>/SiO<sub>2</sub>.

The mean reaction rates observed at the highest (11%) and lowest (0%) O<sub>2</sub> feed fractions studied are summarized in Table 2. The homogeneous reaction of CH<sub>2</sub>O proceeds much more slowly than the reaction in the presence of either solid catalyst.

The rate laws utilized by Arena et al. [11] and Amiridis et al. [13] to describe CH<sub>2</sub>O consumption during CH<sub>4</sub> oxidation over  $SiO_2$  and  $MoO_x/SiO_2$ , respectively, assume that the reaction is oxidative and requires one surface oxygen to proceed (see reactions (2S) and (2M) above). Such rate laws will work as long as the fraction of oxidized surface sites does not vary greatly from the value for the reaction conditions under which the rate constant was determined. However, these rate laws will fail when the distribution of surface species deviates significantly because of changes in coverage by carbonaceous species or oxygen vacancies. A more physically meaningful model for the rate of CH<sub>2</sub>O consumption can be constructed with the incorporation of terms into the rate expressions for CH<sub>2</sub>O consumption accounting for the nonoxidative decomposition of CH<sub>2</sub>O to CO. The following rate laws are therefore proposed to describe the reaction rates of  $CH_2O$  over bare  $SiO_2$  and  $MoO_x/SiO_2$ , respectively:

$$r_{2S} = k_{2S} \, p_{\rm CH_2O},\tag{22}$$

$$r_{\rm 2M} = k_{\rm 2M}^{(0)} p_{\rm CH_2O} \phi_{\rm red} + k_{\rm 2M}^{(1)} p_{\rm CH_2O} \phi_{\rm ox}.$$
 (23)

The rate law for CH<sub>2</sub>O decomposition over SiO<sub>2</sub> is taken to be independent of the speciation of the active sites on SiO<sub>2</sub>, consistent with the observed insensitivity of the reaction rate of CH<sub>2</sub>O to the O<sub>2</sub> partial pressure over bare SiO<sub>2</sub>. The (0) and (1) superscripts on  $k_{2M}$  in Eq. (23) refer to the rate constants for CH<sub>2</sub>O decomposition and oxidation, respectively, on the supported MoO<sub>x</sub> domains. The terms are assumed to represent, respectively, the activities of the reduced (M) sites and oxidized (MO) sites of the supported MoO<sub>x</sub> as presented in the CH<sub>4</sub> oxidation model above.

The rate law for CH<sub>2</sub>O decomposition over SiO<sub>2</sub> (Eq. (22)) was fit to the rate data for CH<sub>2</sub>O over bare SiO<sub>2</sub> at 873 K shown in Fig. 16 by adjustment of the rate constant  $k_{2S}$ . The rate law for CH<sub>2</sub>O reaction over the supported MoO<sub>x</sub> moieties (Eq. (23)) was then fit to the corresponding rate data obtained over MoO<sub>x</sub>/SiO<sub>2</sub> by adjustment of  $k_{2M}^{(0)}$  and  $k_{2M}^{(1)}$ . A surface oxygen balance similar to Eq. (18) was utilized to track the fraction of oxygen vacancies on the supported MoO<sub>x</sub>. The balance was constructed by equating the rate of MoO<sub>x</sub> reduction by CH<sub>2</sub>O and by the H<sub>2</sub> produced from non-oxidative CH<sub>2</sub>O decomposition to the rate of Surface re-oxidation already specified by the fit of CH<sub>4</sub> oxidation data:

 $2r_{\rm 3M} - r_{\rm 2M} - \zeta r_{\rm 2S} = 0. \tag{24}$ 

It was assumed that no carbonaceous species are present on MoO<sub>x</sub> sites during CH<sub>2</sub>O oxidation because CH<sub>2</sub>O is weakly adsorbed on oxides [13,40,41]. Eq. (24) is used together with the site conservation statement given by Eq. (20), taking  $\phi_{\rm C} = 0$ . A similar balance is not necessary for the SiO<sub>2</sub>, since the decomposition of CH<sub>2</sub>O over SiO<sub>2</sub> is independent of the fraction of sites oxidized on SiO<sub>2</sub>. The predictions of the model take into account contributions due to homogeneous reactions and reactions occurring on exposed



Fig. 17. Rate of CH<sub>2</sub>O reaction versus temperature for reaction of CH<sub>2</sub>O over ( $\bullet$ ) bare SiO<sub>2</sub> and (—) model fit by varying  $E_{2S}$ ; ( $\blacksquare$ ) MoO<sub>x</sub>/SiO<sub>2</sub> and (--) model fit by varying  $E_{2M}^{(0)}$  and  $E_{2M}^{(1)}$ . Feed composition was 1.1% CH<sub>2</sub>O, 11.5% O<sub>2</sub> (balance He).

SiO<sub>2</sub> and MoO<sub>x</sub>, as described by Eqs. (5) and (6). The resulting fits of the model are shown with the rate data in Fig. 16. The best fits were obtained with rate constants of  $k_{2S} = 18.3 \,\mu\text{mol}\,\text{cm}^{-3}\,\text{s}^{-1}$ ,  $k_{2M}^{(0)} = 7.91 \,\mu\text{mol}\,\text{cm}^{-3}\,\text{atm}^{-1}\,\text{s}^{-1}$ , and  $k_{2M}^{(1)} = 24.5 \,\mu\text{mol}\,\text{cm}^{-3}\,\text{atm}^{-1}\,\text{s}^{-1}$ .

The O<sub>2</sub> dependence of the homogeneous reaction of CH<sub>2</sub>O appears to account for the very slight increase in the rate of CH<sub>2</sub>O consumption as the O<sub>2</sub> feed fraction is increased over bare SiO2. The dependence of the CH2O reaction rate over  $MoO_x/SiO_2$  with respect to  $O_2$  feed fraction is captured by the model, but the rate rises too sharply with O<sub>2</sub> feed fraction before reaching a plateau. This deviation is the result of a similar trend in fractional oxygen coverage, which rises very sharply with O<sub>2</sub> feed fraction at small  $O_2$  feed fractions because the rate constant  $k_{3M}$  is large relative to the rate constants  $k_{2M}^{(0)}$  and  $k_{2M}^{(1)}$ . Although the fit is not exact, the rate derived from the model deviates by less than 10% on a relative basis over the range of O<sub>2</sub> feed fractions studied. Furthermore, the fit obtained from Eq. (23) is not worse at any O<sub>2</sub> feed fraction than a fit obtained with the use of a rate law that does not include a non-oxidative component and provides a better fit at very small O<sub>2</sub>/CH<sub>2</sub>O ratios where surface oxygen vacancies become significant. As demonstrated in Fig. 12, the fraction of surface vacancies can be quite significant and can vary significantly with gas composition and temperature during CH<sub>4</sub> oxidation.

The temperature dependence of the CH<sub>2</sub>O consumption rate over SiO<sub>2</sub> and over supported MoO<sub>x</sub> was modeled with the assumption that the rate constants  $k_{2S}$ ,  $k_{2M}^{(0)}$ , and  $k_{2M}^{(1)}$  obey Arrhenius expressions, in which the corresponding activation energies are  $E_{2S}$ ,  $E_{2M}^{(0)}$ , and  $E_{2M}^{(1)}$ .  $E_{2S}$  was fit to rate data obtained over bare SiO<sub>2</sub> at various temperatures, and then  $E_{2M}^{(0)}$  and  $E_{2M}^{(1)}$  were fit to similar data obtained over MoO<sub>x</sub>/SiO<sub>2</sub>. The resulting fits of the model to the experimental data are shown in Fig. 17. The activation energies used in the model are  $E_{2S} = 109$  kJ mol<sup>-1</sup>,  $E_{2M}^{(0)} = 125$  kJ mol<sup>-1</sup>, and  $E_{2M}^{(1)} = 120$  kJ mol<sup>-1</sup>. The rate data appear to be well described by Eqs. (22) and (23).

The observations made here allow us to challenge two assertions made in the literature concerning CH<sub>2</sub>O reaction at temperatures relevant to CH<sub>4</sub> oxidation. The first is that the reaction of  $CH_2O$  with  $O_2$  proceeds over  $SiO_2$  by a heterogeneous-homogeneous reaction mechanism, in which the SiO<sub>2</sub> surface initiates the formation of free radicals that decompose  $CH_2O$  in the gas phase [6]. This assertion was based on the observation by mass spectrometry of HO<sub>2</sub>· radicals at a number density of about  $10^{13}$  cm<sup>-3</sup> during the oxidation of CH<sub>2</sub>O over bare SiO<sub>2</sub> at 873 K. Inserting this concentration of  $HO_2$  into the rate law reported by Eiteneer et al. [42] for the decomposition of  $CH_2O$  by  $HO_2$ , we estimate the rate of CH<sub>2</sub>O decomposition at 873 K and 1.5 atm for a feed containing 1% CH<sub>2</sub>O to be 0.01  $\mu$ mol cm<sup>-3</sup> s<sup>-1</sup>. This is about four orders of magnitude less than the rates observed over SiO<sub>2</sub> in the present study, which suggests that the HO<sub>2</sub> · observed by Nersessian et al. is kinetically irrelevant. It can similarly be demonstrated with the use of combustion kinetic data [43] that the concentration of H. necessary to produce the observed concentration of  $HO_2$  · is much too small to decompose CH2O at the observed reaction rate. These conclusions are supported by our observations of the change in the order of reaction with respect to CH<sub>2</sub>O from 2.55 to 1.0 as we go from homogeneous CH<sub>2</sub>O oxidation to heterogeneous CH<sub>2</sub>O oxidation over SiO<sub>2</sub>. The reduction in the reaction order in the presence of  $SiO_2$  may be caused by quenching of the radical mechanism by radical recombination on the SiO<sub>2</sub> surface [9] or simply by the firstorder heterogeneous reaction proceeding at a much greater rate than the higher-order homogeneous reaction.

Bañares and Fierro have also claimed that the reaction of  $CH_2O$  over  $MoO_x/SiO_2$  proceeds primarily in the gas phase based on their observations regarding the deleterious effects of a heated post-reactor volume on the CH2O selectivity during CH<sub>4</sub> oxidation [7]. While homogeneous reaction can indeed destroy an appreciable amount of CH<sub>2</sub>O given sufficient contact time, the present investigation has shown that the void volume within the packed bed is insufficient for the homogeneous reaction to contribute appreciably to the consumption of CH2O for the feed rates studied. Careful attention to reactor design, as described by Bañares and Fierro (exclusion of post-reactor volume and use of small-ID tubing to transport the products rapidly out of the heated zone), is important for minimization of the effects of the homogeneous reaction downstream of the catalyst bed, but within the catalyst the homogeneous component of the reaction appears to be insignificant.

#### 4.5. Model analysis

The kinetic parameters and the rate laws describing the consumption of  $CH_4$  and  $CH_2O$  are summarized in Table 3. This information can now be used to simulate the observed trends in  $CH_4$  conversion and  $CH_2O$  selectivity versus contact time. To utilize the model in a predictive fashion, we cast the surface oxygen balances in terms of the rates of surface

Summary of k	cinetic parameters					
Rate	Kinetic	Rate constant at 873 K			Pre-exponential	Activation
constant	group	k <sub>i</sub> (873 K)	<i>k</i> <sup>'</sup> <sub>1</sub> (873 K)	k'' (873 K)	factor, $A_i$	energy, E <sub>i</sub>
$CH_4 \rightarrow CH_2($	0					
č1S	$p_{\mathrm{CH}_4}  heta_{\mathrm{ox}}^2$	$0.122 \ \mu mol \ cm^{-3} \ atm^{-1} \ s^{-1}$	$0.466 \mathrm{nmol}\mathrm{m}^{-2}\mathrm{atm}^{-1}\mathrm{s}^{-1}$	1	$145 \text{ mol cm}^{-3} \text{ atm}^{-1} \text{s}^{-1}$	$152 \text{ kJ mol}^{-1}$
<sup>c</sup> OMf	$P C H_4 \phi_{OX}$	$1.35 \ \mu mol \ cm^{-3} \ atm^{-1} \ s^{-1}$	I	$6.44 \times 10^{-3} \text{ mol mol}_{Mo}^{-1} \text{ atm}^{-1} \text{s}^{-1}$	$2.86 \times 10^{6} \mathrm{ \ mol \ cm^{-3} \ atm^{-1} \ s^{-1}}$	$206 \text{ kJ mol}^{-1}$
<sup>c</sup> OMr	$\phi_{C}\phi_{H}$	710 $\mu$ mol cm <sup>-3</sup> s <sup>-1</sup>	1	$3.39 \text{ mol mol}_{M_0}^{-1} \text{ s}^{-1}$	$5.72 \times 10^{14} \mathrm{mol}\mathrm{cm}^{-3}\mathrm{s}^{-1}$	$299 \text{ kJ mol}^{-1}$
k1M	φοχφC	$40.6 \ \mu mol \ cm^{-3} \ s^{-1}$	I	$0.194 \text{ mol mol}_{M_0}^{-1} \text{ s}^{-1}$	$4.77 \times 10^{11} \mathrm{mol} \mathrm{cm}^{-3} \mathrm{s}^{-1}$	$269 \text{ kJ mol}^{-1}$
$CH_2O \rightarrow CO$	,r					
<sup>k</sup> 2H	$p_{ m CH_2O}^{2.65} D_{ m O_2}^{0.55}$	$5.2 \times 10^{-3} \ \mu mol \ cm^{-3} \ atm^{-3.16} \ s^{-1}$	I	I	$3.54 \times 10^{11} \mathrm{\ mol\ cm^{-3}\ atm^{-3.16}\ s^{-1}}$	$231 \text{ kJ mol}^{-1}$
¢2S	$PCH_2O$	$18.3 \ \mu mol \ cm^{-3} \ atm^{-1} \ s^{-1}$	$58.3 \text{ nmol m}^{-2} \text{ atm}^{-1} \text{ s}^{-1}$	1	$57.3 \text{ mol cm}^{-3} \text{ atm}^{-1} \text{s}^{-1}$	$109 \text{ kJ mol}^{-1}$
(0) 2M	$P_{CH_2O\phi_{red}}$	$7.91 \text{ µmol cm}^{-3} \text{ atm}^{-1} \text{s}^{-1}$	I	$0.0390 \text{ mol mol}_{M_{O}}^{-1} \text{ atm}^{-1} \text{s}^{-1}$	$237 \text{ mol cm}^{-3} \text{ atm}^{-1} \text{s}^{-1}$	$125 \text{ kJ mol}^{-1}$
$\epsilon_{2M}^{(1)}$	$PCH_2O\phi_{\rm ox}$	$24.5 \ \mu mol \ cm^{-3} \ atm^{-1} s^{-1}$	1	$0.117 \text{ mol mol}_{M_0}^{-1} \text{ atm}^{-1} \text{s}^{-1}$	$1690 \text{ mol cm}^{-3} \text{ atm}^{-1} \text{s}^{-1}$	131 kJ mol <sup>-1</sup>
M → MO						
<sup>¢3S</sup>	$P_{02}\theta_{\mathrm{red}}^2$	$50.3 \ \mu mol \ cm^{-3} \ atm^{-1} s^{-1}$	$192 \text{ nmol m}^{-2} \text{ atm}^{-1} \text{s}^{-1}$	1	$5.03 \times 10^{-5} \text{ mol cm}^{-3} \text{ atm}^{-1} \text{ s}^{-1}$	$0 \text{ kJ mol}^{-1}$
k3M	$p_{\rm O_2} \phi_{\rm red}^2$	$178 \ \mu mol \ cm^{-3} \ atm^{-1} \ s^{-1}$	I	$0.850 \text{ mol mol}_{Mo}^{-1} \text{ atm}^{-1} \text{ s}^{-1}$	$3.80 \times 10^{-3} \text{ mol cm}^{-3} \text{ atm}^{-1} \text{ s}^{-1}$	$22.2 \text{ kJ mol}^{-1}$

Table 3



Fig. 18. CH<sub>4</sub> conversion and CH<sub>2</sub>O selectivity during CH<sub>4</sub> oxidation over bare SiO<sub>2</sub> at 873 K with feed consisting of 90% CH<sub>4</sub>, 10% O<sub>2</sub>. ( $\blacklozenge$ ) Observed CH<sub>4</sub> conversion and (—) model prediction; ( $\blacktriangle$ ) observed CH<sub>2</sub>O selectivity and (---) model prediction.

reduction and oxidation, rather than in terms of the parameter  $n_i$ . The balance on oxidized MoO<sub>x</sub> sites (Eq. (18)) is re-written as

$$2r_{3M} - r_{0Mf} + r_{0Mr} - r_{1M} - \left(\frac{S_{CO} + 2S_{CO_2}}{S_{CO} + S_{CO_2}}\right)r_{2M} - \zeta r_{2S} = 0.$$
(25)

The CH<sub>2</sub>O consumed by non-oxidative processes over both exposed SiO<sub>2</sub> and supported  $MoO_x$  is accounted for in the  $MoO_x$  oxygen balance because the H<sub>2</sub> produced by these processes is oxidized to  $H_2O$  over  $MoO_x$ . The bracketed term in Eq. (25) accounts for the additional surface oxygen consumed in the generation of CO<sub>2</sub>. The product distribution during the oxidation of  $CH_2O$  over  $MoO_x/SiO_2$  is typically 90% CO, 10% CO<sub>2</sub>, so the bracketed term is approximated as 1.1. This is a good approximation because the term varies weakly with the product distribution (going from 1.1 at a  $CO/CO_2$  ratio of 9 to 1.2 at a  $CO/CO_2$  ratio of 6). At contact times shorter than the time of maximum CH<sub>2</sub>O yield, this assumption is even more appropriate because the rate of CH<sub>4</sub> oxidation is faster than the rate of CH<sub>2</sub>O consumption. For  $SiO_2$ , it was possible to continue using Eq. (13) with  $n_{\rm S} = 1$ , since CH<sub>2</sub>O decomposition does not consume surface oxygen.

Comparisons of the model predictions with experimental data observed during CH<sub>4</sub> oxidation over bare SiO<sub>2</sub> are shown in Fig. 18. Consumption of both CH<sub>4</sub> and CH<sub>2</sub>O appears to occur somewhat more slowly over the bare SiO<sub>2</sub> than is predicted by the model. The predicted CH<sub>4</sub> conversion is about 33% higher than the observed rate at a contact time of 1.25 s, and the predicted CH<sub>2</sub>O selectivity is about 33% lower than the observed selectivity. The model predictions are better at shorter times. The deviation may be due in part to experimental error and may also be related to the variation in H<sub>2</sub>O partial pressure with contact time, as H<sub>2</sub>O is unaccounted for in the model and may in fact inhibit CH<sub>4</sub> oxidation. Because the rate of CH<sub>4</sub> oxidation over SiO<sub>2</sub> is small relative to the corresponding rate over supported MoO<sub>x</sub>, this deviation is not of great concern. It



Fig. 19. CH<sub>4</sub> conversion and CH<sub>2</sub>O selectivity during CH<sub>4</sub> oxidation over  $MoO_x/SiO_2$  at 873 K with feed consisting of 90% CH<sub>4</sub>, 10% O<sub>2</sub>. ( $\blacklozenge$ ) Observed CH<sub>4</sub> conversion and (—) model prediction; ( $\blacktriangle$ ) observed CH<sub>2</sub>O selectivity and (---) model prediction.



Fig. 20. Model predictions of maximum  $CH_2O$  yield with respect to contact time versus  $CH_4$  feed fraction at various temperatures.  $O_2$  feed fraction held constant at 10%, total pressure of 1.5 atm absolute.

should be noted that the predicted  $CH_2O$  selectivity versus  $CH_4$  conversion is excellent, as the observed rate of  $CH_2O$  decomposition (as measured by the  $CH_2O$  selectivity) is slower by approximately the same factor as the observed rate of  $CH_4$  oxidation.

The predicted trends for CH<sub>4</sub> oxidation over  $MoO_x/SiO_2$ at 873 K with 90% CH<sub>4</sub>, 10% O<sub>2</sub> are compared with the observed data in Fig. 19. The model predictions are in very good agreement with observations of both CH<sub>4</sub> conversion and CH<sub>2</sub>O selectivity over the entire range of the data. Deviations are less than 10 relative % over the entire range.

Since the model provides a good description of CH<sub>4</sub> conversion and CH<sub>2</sub>O selectivity for  $MoO_x/SiO_2$  and was developed from observations made over a wide range of temperatures and gas-phase compositions, it can be used to assess the impact of reaction conditions on the CH<sub>2</sub>O yield. Fig. 20 shows the effects of both feed composition and temperature on the maximum single-pass yield achievable with respect to contact time over  $MoO_x/SiO_2$ . The highest single-pass yields are possible when the rate of CH<sub>4</sub> oxidation is maximized relative to the rate of CH<sub>2</sub>O consumption. The rate of CH<sub>4</sub> oxidation is more sensitive to the fraction of oxidized sites than is the rate of reaction of oxidized sites



Fig. 21. Mean rates of CH<sub>4</sub> oxidation and CH<sub>2</sub>O consumption in each of the reactive media versus contact time at 923 K, 1.5 atm during CH<sub>4</sub> oxidation with feed composed of 20% CH<sub>4</sub>, 10% O<sub>2</sub> (balance He). The slope of the top curve in each plot is the total local rate. The maximum CH<sub>2</sub>O yield occurs at 0.29 s under these conditions, where the total local rates of CH<sub>4</sub> oxidation and CH<sub>2</sub>O consumption are equal.

over the exposed SiO<sub>2</sub> and pseudo-second-order in the fraction of oxidized sites over  $MoO_x$ , whereas reaction of  $CH_2O$ is independent of the fraction of oxidized sites over SiO<sub>2</sub> and first-order in the fraction of oxidized sites over  $MoO_x$ . Hence the maximum single-pass yield achievable increases with decreasing  $CH_4/O_2$  ratio as the surface fractions of oxidized sites become greater. At 923 K, the maximum possible CH<sub>2</sub>O yield increases from 2.0 to 5.1% as the CH<sub>4</sub> feed fraction is decreased from 90 to 1% while the O<sub>2</sub> feed fraction is held constant at 10%. Because the activation energies for CH<sub>4</sub> oxidation are large relative to the activation energies for CH<sub>2</sub>O decomposition and oxidation, the rate of CH<sub>4</sub> oxidation increases faster than the rate of CH2O consumption with increasing temperature, so the maximum possible yield increases with temperature. This effect is much more pronounced at small CH<sub>4</sub>/O<sub>2</sub> ratios. High CH<sub>4</sub>/O<sub>2</sub> ratios diminish the effect of increasing temperature, as the balance of surface sites is shifted away from oxidized sites under these conditions. With a feed composed of 1% CH<sub>4</sub>, 10% O<sub>2</sub>, the maximum CH<sub>2</sub>O yield increases from 2.2% at 848 K to 7.8% at 973 K, but with a feed composed of 90% CH<sub>4</sub>, 10% O<sub>2</sub>, the maximum CH<sub>2</sub>O yield only increases from 1.2 to 2.0%. This is consistent with the observations of Spencer and Pereira, who observed only a very slight increase in the profile of CH<sub>2</sub>O selectivity versus CH<sub>4</sub> conversion with increasing temperature when they conducted experiments at a  $CH_4/O_2$  ratio of 9 [14].



Fig. 22. Maximum CH<sub>2</sub>O yield with respect to contact time versus CH<sub>4</sub>:O<sub>2</sub> ratio for CH<sub>4</sub> oxidation at 973 K, 1.5 atm with 10% O<sub>2</sub> feed fraction over  $MoO_x/SiO_2$ . (—) All reaction pathways active (real system as modeled); (---) SiO<sub>2</sub> pathways inactive.

Having defined the contributions of the gas-phase, support, and supported  $MoO_x$ , it is possible to isolate the intrinsic activity of the supported  $MoO_x$ . Fig. 21 shows the contribution of each locus of reaction on the total rates of reaction during CH<sub>4</sub> oxidation at 923 K for a feed composed of 20% CH<sub>4</sub>, 10% O<sub>2</sub>. These contributions were determined by constructing the gas-phase and surface species profiles versus contact time, integrating the local rates of reaction in each of the reactive media over the length of the reactor, and normalizing by the total contact time. The observed rate of reaction is the sum over  $\langle r_i \rangle$  for reaction occurring in the gas phase, on the exposed SiO<sub>2</sub>, and on the supported MoO<sub>x</sub>.

$$\langle r_i \rangle = \frac{1}{\tau} \int_0^\tau r_i(\tau') \,\mathrm{d}\tau'. \tag{26}$$

The overall rate of reaction is given by the uppermost curve in Fig. 21. The rate of reaction at a given contact time within the reactor is proportional to the slope of the uppermost curve, and the maximum yield is obtained when the slopes of the CH<sub>2</sub>O consumption rate and CH<sub>4</sub> oxidation rate are equal but opposite. This occurs at  $\tau = 0.29$  s for the conditions shown in Fig. 21. At this contact time, the mean  $CH_4$  oxidation rate over the supported  $MoO_x$  is 1.17  $\mu$ mol cm<sup>-3</sup> s<sup>-1</sup>, whereas the mean rate of CH<sub>4</sub> oxidation over the exposed SiO<sub>2</sub> is only 0.082  $\mu$ mol cm<sup>-3</sup> s<sup>-1</sup>. The mean rates of CH<sub>2</sub>O consumption at this contact time are 0.483, 0.358, and 0.041  $\mu$ mol cm<sup>-3</sup> s<sup>-1</sup> on the MoO<sub>x</sub>, on the exposed SiO<sub>2</sub>, and in the gas-phase, respectively. Hence the effect of the exposed SiO<sub>2</sub> on the observed activity is deleterious, as it contributes to the consumption of CH<sub>2</sub>O to a greater extent than it does to the formation of CH<sub>2</sub>O.

To determine the activity of  $MoO_x$  on a completely inert support, the rates of the reactions over SiO<sub>2</sub> are set to zero in the model. The resulting increase in the maximum CH<sub>2</sub>O yield with respect to contact time is plotted in Fig. 22 versus the CH<sub>4</sub> feed fraction at 973 K while the O<sub>2</sub> feed fraction is held constant at 10%. When a completely inert support is used, the maximum CH<sub>2</sub>O yield increases from 7.8 to 10.5% at 1% CH<sub>4</sub>, or from 2.0 to 2.5% at 90% CH<sub>4</sub>.

# 5. Conclusions

A model has been developed to describe the kinetics of the selective oxidation of methane to formaldehyde over  $MoO_x/SiO_2$ . This model accounts for the reactions of methane and formaldehyde occurring in the gas phase and on the surfaces of the silica support and the dispersed molybdena. The overall rate of reaction, predicted by the model as the sum of the rates of reaction proceeding in the gas phase and on the catalyst surface, very accurately describes the rate of CH<sub>4</sub> oxidation and the selectivity of the products for CH<sub>2</sub>O observed experimentally. Since the kinetics of homogeneous reaction and heterogeneous reaction occurring on SiO<sub>2</sub> and MoO<sub>x</sub> are each known, it is possible to use the model to assess the importance of each contribution to the overall performance of the catalyst.

The oxidation of CH<sub>4</sub> is found to proceed almost exclusively over the supported molybdena. The rate of homogeneous oxidation is negligible at the pressures used in this study, and the rate of CH<sub>4</sub> oxidation over bare SiO<sub>2</sub> is about an order of magnitude less than that over the supported MoO<sub>x</sub>. Although the rate of gas-phase CH<sub>2</sub>O oxidation is measurable, the void volume within the catalyst is insufficient for this process to make a significant contribution to overall rate of CH<sub>2</sub>O consumption. The principal process occurring over bare SiO<sub>2</sub> is CH<sub>2</sub>O decomposition to form CO and H<sub>2</sub>. Even in the presence of excess O<sub>2</sub>, very little of the H<sub>2</sub> undergoes combustion. CH<sub>2</sub>O decomposition also occurs on the supported MoO<sub>x</sub>. When O<sub>2</sub> is present in the feed, all of the H<sub>2</sub> formed from CH<sub>2</sub>O decomposition is combusted on the supported MoO<sub>x</sub>.

The maximum single-pass conversion of CH<sub>4</sub> to CH<sub>2</sub>O is strongly influenced by temperature and CH<sub>4</sub>/O<sub>2</sub> ratio in the feed. The maximum single-pass yield increases with increasing temperature and decreasing CH<sub>4</sub>/O<sub>2</sub> ratio. For the catalyst studied a maximum CH<sub>2</sub>O yield of 7.0% could be achieved at a temperature of 973 K with a feed composed of 5% CH<sub>4</sub> and 10% O<sub>2</sub> in He. A further gain of 2.5% could be achieved if the surface of SiO<sub>2</sub> were made completely inactive.

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